





$$\begin{aligned}
 \sin(\theta_4) &= \sin(\theta_{out} - \theta_b) = \sin(\theta_{out}) - \cos(\theta_{out})\theta_b \\
 &= n \cdot \sin(\theta_3) = n \cdot \sin(\theta_2 - 2\beta) = n \cdot (\sin(\theta_2) - 2\beta \cos(\theta_2))
 \end{aligned}$$

$$\sin(\theta_1) = n \cdot \sin(\theta_2)$$

$$\sin(\theta_{out}) = \sin(\theta_1)$$

$$\begin{aligned}
 \theta_b &= 2\beta n \cos(\theta_2) / \cos(\theta_{out}) \\
 &= 2\beta \sqrt{n^2 - \sin(\theta_1)^2} / \cos(\theta_{out}) \\
 &= 3.55\beta = 0.0043
 \end{aligned}$$