

Radiation Pressure for reflected light in FP

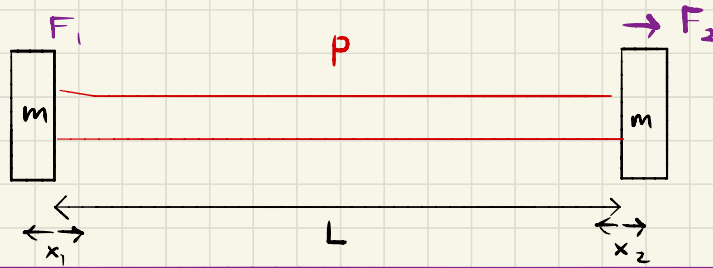
$$F = \frac{2P}{c}$$

$$x_i = -\frac{F_i}{m\omega^2}$$

$$\Delta L = x_1 - x_2 \approx 2\Delta x$$

$$= -\frac{2\Delta F}{m\omega^2}$$

$$\Delta L = -\frac{4\Delta P}{m\omega^2}$$



Now, $L_{\text{DARM}} = L_x - L_y$, so

$$\Delta L_D = -\frac{4}{m\omega^2} (\Delta P_x - \Delta P_y)$$

For an intensity noise injection, the change in the power in each arm can be written as

$$\Delta P_x = \text{RIN}_a(f) P_x, \quad \Delta P_y = \text{RIN}_a(f) P_y$$

$$\Rightarrow \frac{L_{\text{DARM}}(f)}{\text{RIN}_a(f)} = -\frac{4}{m\omega^2} (P_x - P_y) = -\frac{4}{m\omega^2} \Delta P_{\text{arms}}$$

Finally, $\text{RIN}_a(f)$ is the RIN of the arms, and is cleaned relative to the input RIN via the CARM pole: $\frac{\text{RIN}_{\text{arms}}}{\text{RIN}_{\text{input}}} = \frac{1}{1 + i\frac{\omega}{\omega_{\text{CARM}}}}$

$$\frac{L_{\text{DARM}}(f)}{\text{RIN}_{\text{input}}(f)} = -\frac{4}{m\omega^2} \frac{1}{1 + i\frac{\omega}{\omega_{\text{CARM}}}} \Delta P_{\text{arms}}$$